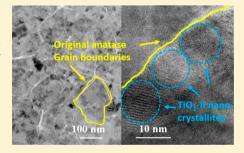


High-Pressure Phase Transitions in Densely Packed Nanocrystallites of TiO₂-II

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Supporting Information

ABSTRACT: Phase behaviors of nanocrystalline TiO2-II have not been well studied due to the difficulty in its preparations at ambient pressure. In this work, we prepared nanocrystallites of TiO2-II with average sizes of ~10-20 nm via high-pressure processing of anatase particles in a large volume press. X-ray diffraction (XRD) and electron microscopy examinations show that the TiO₂-II nanocrystallites formed from cracking and phase transformation of large anatase particles under compression. The high-pressure phase behaviors of the TiO₂-II nanocrystallites were investigated using in situ synchrotron XRD and Raman spectroscopy. Results show that, under compression up to ~35-40 GPa, the phase transitions in nano TiO₂-II proceed via two parallel routes of TiO₂-II (~9– 15 GPa) \rightarrow baddeleyite (~25 GPa) \rightarrow TiO₂-OI and TiO₂-II (~19 GPa) \rightarrow



TiO₂-OI. At different TiO₂-II sizes, the TiO₂-II-to-baddeleyite transition occurs at pressures from ~9 to 15 GPa, while the TiO₂-II-to-TiO₂-OI transition occurs at ~19 GPa. This difference originates from the different interfacial energies of the involved titania phases, which control their relative thermodynamic phase stabilities at nano sizes. This work enriches our understanding of the complex phase behaviors of titania and provides fundamental knowledge for developing applications of the less-explored titania nanophase of TiO₂-II.

1. INTRODUCTION

Titania (TiO₂) finds applications in photocatalysis, ¹⁻³ coatings, 4 electronic components, 5,6 thermal insulations, 7 etc. TiO₂ has more than 10 polymorphs⁸ that include the ambient phases rutile, anatase, brookite, $TiO_2(B)$, $TiO_2(H)$, $TiO_2(H)$ and $TiO_2(R)$ and the high-pressure phases with the structure types of α -PbO₂ (i.e., TiO₂-II, space group *Pbcn*, ICSD no. 15328¹²), baddeleyite (space group P2₁/c, COD no. 9015355¹³), orthorhombic-I (TiO2-OI, space group Pbca, COD no. 9004140¹³), fluorite, 14 cotunnite (TiO₂-OII, space group Pnma, ICSD no. 27736¹²), and Fe₂P. It was demonstrated recently that the TiO2-II phase may have promising applications in photocatalytic and electrocatalytic hydrogen generation 16,17 and in optical and optoelectronic devices due to its high refractive index. 18 Previous studies show that, under compression up to ~70 GPa, bulk anatase, rutile, and brookite experience the same transition route from bulk TiO₂ phase → TiO_2 -II phase \rightarrow baddeleyite phase \rightarrow TiO_2 -OI phase \rightarrow

TiO₂-OII phase. 19-22 For nanocrystals of titania, the pressureinduced phase transition is dependent on particle size, morphology, and temperature. 23-29 For example, anatase nanocrystals with sizes < ~10 nm transform to an amorphous state at P > 27 GPa and those with sizes between ~ 12 and 50 nm transform to the baddelevite phase at P > 18 GPa.²⁷ In comparison, bulk anatase crystals transform to TiO2-II at P > 4.5 GPa.³⁰ Interestingly, in decompression to ambient pressure, all high-pressure phases transform to (or retain) the TiO2-II phase, irrespective of the structures and sizes of the starting phases (e.g., anatase, rutile, or brookite), 19-31 with the exception that an amorphous phase may be produced in a rapid decompression of titania crystallites having sizes <8 nm.²⁴ However, so far, the high-pressure behavior of

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nanocrystalline TiO_2 -II has been scarcely studied because of the difficulty in synthesizing nano TiO_2 -II at ambient pressure. Nonetheless, such a knowledge on the phase behavior of nano TiO_2 -II is highly needed for making good use of its material properties for novel applications, such as for photocatalysis and electrocatalysis. Thus, in this work, we used in situ highpressure (HP) X-ray diffraction (XRD) and HP-Raman spectroscopy to study the structural changes of TiO_2 -II nanocrystallites produced from high-pressure processing. Further, we analyzed the size-dependent phase transition behaviors of TiO_2 -II using thermodynamics. The obtained knowledge will be indispensable for exploiting new applications of nano TiO_2 -II.

2. EXPERIMENTAL SECTION

2.1. Chemicals. Three titanium dioxide (in anatase phase) powders with factory-labeled particle sizes of 40 nm (99.8% wt), 120 nm (99.8% wt), and $2-3 \mu m$ (99% wt) were purchased from Macklin Biochem. Co. Ltd. (Shanghai).

2.2. Preparation of TiO₂-II Samples under High-Pressure and High-Temperature (HPHT) Conditions. TiO2-II samples were prepared from HPHT processing of anatase powders using a multianvil large-volume press (LVP) (Mavo Press LP1000). First, about 0.1 g of powders of a purchased anatase chemical were loaded to the sample chamber (diameter 3 mm) of a zirconia octahedron with a length of 8 mm. Then, the octahedron was assembled to the LVP. The pressure of the LVP was calibrated using the resistance changes associated with the high-pressure phase transitions of ZnS and GaAs.³² After compressing the sample to ~15 GPa, the temperature was ramped from room temperature to 350 °C at a rate of 50 °C/min and kept at the temperature for 2 h. Then, the sample was quenched to ambient temperature and pressure. The final product was shaped in a compacted rod ($\sim \phi$ 2.5 mm \times L3 mm) consisting of TiO₂-II nanocrystallites (see below). The average crystallite size (see below) of the TiO2-II sample derived from the factory-labeled "120 nm" anatase was 10.7 nm (herein denoted as sample #1), that from the factory-labeled "2-3 μ m" anatase was 17.9 nm (denoted as sample #2), and that from the factory-labeled "40 nm" anatase was 20.2 nm (denoted as sample #3).

2.3. Characterizations of Raw Anatase Samples and As-Prepared TiO₂-II Samples. XRD patterns of the raw anatase samples and the as-prepared TiO₂-II samples were collected using an X-ray diffractometer (Malvern Panalytical) operated at 40 kV and 40 mA, with a Cu K α radiation (X-ray wavelength 1.54056 Å). The average crystallite sizes of the samples were derived from Rietveld fitting using the Maud program. 33,34

The morphologies of the crystallites contained in the samples were examined using a scanning electron microscope (SEM) (FEI Versa 3D dual-beam FIB/SEM) operated at 5.0 kV. The elemental distributions in the samples were mapped using energy dispersive spectroscopy (EDS) of the SEM operated at 15.0 kV. The focused ion beam (FIB) accessory of the SEM was used to prepare the specimen for observing the microstructures of the TiO₂-II crystallites using a transmission electron microscope (TEM). The TiO₂-II nanocrystallites contained in the as-prepared TiO₂-II samples and the samples quenched from chosen high pressures (see below) were examined using a JEOL 2100 TEM operated at 200 kV.

2.4. Phase Behavior of TiO_2 -II by in Situ High-Pressure X-ray Diffraction. A diamond anvil cell (DAC) was used to generate high pressures on a studied sample. The culet size (diameter) of the anvils was 300 μ m. A T301 stainless steel gasket was preindented to ~30 μ m in thickness using the DAC, and a hole of ~120 μ m in diameter was drilled through the center of the indentation using a laser mill, serving as the sample chamber. Another DAC with a culet size of 600 μ m was used to compress a sample to ~15 μ m in thickness. A piece of thus compressed sample ~40 μ m in diameter was picked out and loaded into the sample chamber of the first DAC together with two small grains of ruby as the pressure calibrant. Then, neon as the pressure transmitting medium was loaded into the sample chamber using a gas-loading system.

High-pressure XRD of the 10.7 nm TiO_2 -II sample #1 (at P up to 35.3 GPa) was performed at the BL15U1 beamline station of Shanghai Synchrotron Radiation Facility (SSRF) at room temperature. XRD patterns were collected at a photon energy of 20 keV (wavelength 0.6199 Å) using a MAR165 CCD detector. The sample-to-detector distance was calibrated using a CeO_2 powder standard.

High-pressure XRD of the 17.9 nm $\rm TiO_2\text{-}II$ sample #2 (at *P* up to 41.5 GPa) was performed at the experimental station 13-BM-C at the GSECARS beamline of Advanced Photon Source (APS). The diffraction was performed at room temperature. XRD patterns were collected at a photon energy of 28.6 keV (wavelength 0.4340 Å) using a MAR165 CCD detector. The sample-to-detector distance and the detector tilt were calibrated using a NIST LaB₆ powder standard.

High-pressure XRD of the 20.2 nm $\rm TiO_2$ -II sample #3 (at *P* up to 40.1 GPa) was performed at beamline 12.2.2 station of Advanced Light Source (ALS) at room temperature. XRD patterns were collected at a photon energy of 25 keV (wavelength 0.4959 Å) using a MAR345 image plate detector. The sample-to-detector distance was calibrated using a $\rm CeO_2$ powder standard.

All diffraction images were converted to the intensity versus 2θ data using the Dioptas program. Then, the phases present, the phase contents, and the lattice parameters of all involved TiO₂ phases were identified and/or derived from Rietveld analyses of the XRD data using the Maud program. 33,34

2.5. Phase Behaviors of TiO_2 -II by in Situ High-Pressure Raman Spectroscopy. Raman spectroscopy of TiO_2 -II samples at high pressure (up to ~42 GPa) was measured at room temperature using a Raman spectrometer (inVia Refiex, Renishaw) with a 532 nm-wavelength excitation laser. For a sample at a given pressure, a laser beam of ~10 μ m in diameter was focused at chosen locations of the sample in the DAC and the spectra in the Raman shift range of 100–1250 cm⁻¹ were collected and then averaged.

3. RESULTS

3.1. Average Crystallite Sizes of Raw Anatase Samples. The average crystallite sizes (see Table S1, Supporting Information) of the three raw anatase samples were estimated to be 35.0, 326.9, and 416.0 nm based on Rietveld fitting of the XRD patterns (see Figure S1a-d). The latter two sizes (>100 nm) are regarded as inaccurate due to use of narrow XRD peak broadening in the size estimations.³⁷ To compensate for this shortcoming, SEM images (Figure S2a-c) were used to estimate the average sizes of the crystallites contained in each of the three samples, as listed in

Table S1. It is seen that the nominally 40 nm-sized sample shows good agreement of the SEM size (34.5 nm) with the Rietveld-derived size (35 nm). The medium-sized sample (nominally 120 nm) was measured by SEM to be 122.0 nm, i.e., very close to the nominal size. However, the factory-labeled "2–3 μ m" anatase actually has an average crystallite size of 117.5 nm, as determined by SEM. The factory-labeled size might be the aggregate size of anatase nanoparticles.

3.2. Average Crystallite Sizes of As-Prepared TiO2-II **Samples.** The average crystallite sizes of the three as-prepared TiO_2 -II samples (see Table S2) were estimated to be 10.7 \pm 0.1 nm (sample #1), 17.9 \pm 0.2 nm (sample #2), and 20.2 \pm 0.1 nm (sample #3) based on Rietveld fitting of the XRD patterns (see Figure S3). TEM images (Figure S4) show that the TiO2-II samples consisted of densely packed nanocrystallites of TiO2-II due to application of high pressure during the HPHT syntheses, and the estimated crystallite sizes $[\sim (10-20) \pm (2-4) \text{ nm}]$ and size distributions (Figure S4d) are in good agreement with those derived from the XRD data (Table S2). The crystallite sizes of the prepared TiO₂-II samples (~10-20 nm; Figure S4) are much smaller than those of the raw anatase particles (average size \sim 35–120 nm; Figure S2) owing to cracking of the bigger raw anatase crystallites under compression and their subsequent phase transformation to TiO₂-II. It is interesting to note that the smaller the raw anatase crystallites are, the larger the derived TiO2-II nanocrystallites are (Table S2). This may be attributed to the reduced compressibility and hence the enhanced deformation strength of smaller anatase particles.

The morphologies of the grains contained in the three asprepared TiO_2 -II samples are shown in the SEM images in Figure S5a-c, and the EDS spectra and the elemental mapping of the samples are shown in Figure S5d-f. As with the TEM images (Figure S4a-c), the SEM images show the compacting structure of grains in the as-prepared TiO_2 -II samples. EDS spectra show that the TiO_2 -II samples consisted of Ti and O atoms with an atomic ratio of $Ti:O \approx 1:2$, while EDS elemental mapping shows that Ti and O are uniformly distributed in the samples.

3.3. High-Pressure Phase Behavior of As-Prepared 10.7 nm TiO₂-II. The XRD patterns of the originally 10.7 nm TiO_2 -II (sample #1) at high pressure is shown in Figure 1. It is seen that XRD peaks broaden significantly and, in many cases, overlap with each other due to the small sizes of the involved titania phases. This hinders direct identifications of the phases present. Thus, visual inspections were combined with Rietveld fitting to identify the phases. Representative Rietveld fittings are shown in Figure S6, and the obtained phase contents and lattice parameters are listed in Table S3. Results show that, in compressing to 4.1 GPa, the sample remained as a single phase of TiO2-II. As the pressure increased to 12 GPa, the baddeleyite phase started to occur. The content of the baddeleyite phase continued to increase with increasing pressure up to the highest experimental value of 35.3 GPa. When the pressure was increased to 21.1 GPa, the TiO2-OI phase appeared, which remained up to 35.3 GPa. On the other hand, the TiO2-II phase disappeared at 25.8 GPa. The observed coexistence of baddeleyite and TiO2-OI at 25.8-35.3 GPa may be attributed to the similarities between the two phases.^{39,40} This is because, as shown in Figure 2, both phases comprise regular or slightly distorted augmented triangular prisms⁸ each of which consists of one Ti atom coordinated by seven O atoms (Figure 2a,c), and both phases produce similar

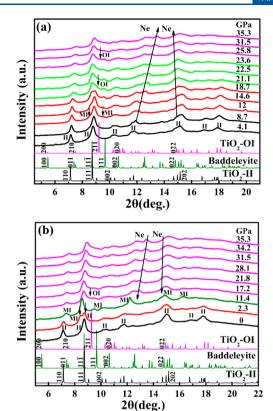


Figure 1. High-pressure XRD patterns of the originally 10.7 nm TiO_2 -II (sample #1) under compression (a) and decompression (b) using neon as the pressure transmitting medium. Calculated XRD patterns of TiO_2 -II, baddeleyite, and TiO_2 -OI are shown at the bottom for comparison. The X-ray wavelength is 0.4340 Å. II = TiO_2 -II, MI = baddeleyite, OI = TiO_2 -OI.

motifs with open channels along the [001] direction (Figure 2b,d). In decompression, the ${\rm TiO_2}$ -OI phase fully converted back to the baddeleyite phase at 11.4 GPa, which converted back to the ${\rm TiO_2}$ -II phase after decompression to \sim 0 GPa. These show that the high-pressure phase transitions in ${\rm TiO_2}$ -II are reversible.

HP-Raman data (Figure 3) are further used to examine the high-pressure phase transitions in the originally 10.7 nm TiO₂-II. As shown in Figure 3a, the Raman peaks at 0.2 GPa are in good agreement with the predicted vibrational bands of TiO2-II. 41 When the pressure was increased to 7.6 GPa, a new Raman peak (~194 cm⁻¹) appeared. This indicates the start of the transition from TiO2-II to baddeleyite, as this B₁₁ phonon mode of TiO2-II associates closely with the atomic displacements in TiO2-II in its transformation to the baddeleyite phase.⁴¹ As the pressure increased to 13.3 GPa, several weak peaks appeared at 219.1, 241.6, and 267.4 cm⁻¹, originating from the characteristic vibrational modes of the baddeleyite phase.^{23,41} Upon further compression to 20.4 GPa, the Raman peaks of the TiO2-OI phase started to occur, while those of the TiO₂-II phase became weak and then almost disappeared at 30.5 GPa. From 30.5 to 40.9 GPa, the Raman spectra contain contributions from both the baddeleyite and TiO₂-OI phases. In decompression (Figure 3b), when the pressure was decreased from 40.9 to 14.1 GPa, the Raman peaks of TiO₂-OI progressively weakened, while those of baddeleyite increased. On further decompression to 12.3 GPa, the Raman peaks were almost all due to the baddeleyite phase. As the pressure was decreased to 3.2 GPa, Raman peaks of

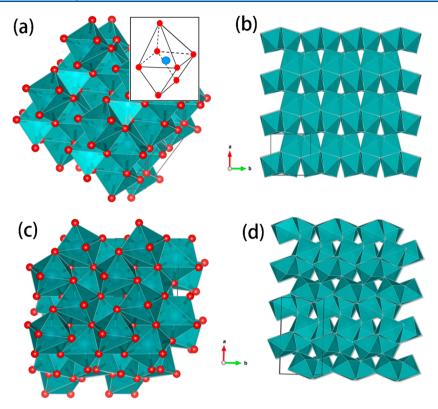


Figure 2. Polyhedron representations of the crystal structures of baddeleyite (a, b) and TiO_2 -OI (c, d). Baddeleyite comprises augmented triangular prisms each of which is made of one Ti atom and seven O atoms (a) (see the inset). TiO_2 -OI also comprises augmented triangular prisms that are slightly distorted (c). When looking down the [001] direction, both structures produce similar motifs (b, d), indicating their structural similarities.

 ${\rm TiO_2}$ -II became obvious. After the sample is released to the ambient environment (\sim 0 GPa), the Raman spectra can be attributed fully to the single ${\rm TiO_2}$ -II phase. The observed phase behaviors from the HP-Raman spectroscopy are in good agreement with those from the HP-XRD experiment (above).

3.4. High-Pressure Phase Behavior of As-Prepared 17.9 nm TiO₂-II. As shown in Figure 4a, at high pressure, the phase behaviors of the originally 17.9 nm TiO₂-II (sample #2) are similar to those of the originally 10.7 nm TiO₂-II (sample #1; above). Again, visual inspection combined with Rietveld fitting (Figure S7) was used to identify the phases present and to obtain the phase contents (Table S4). In compression (Figure 4a), the TiO₂-II phase was observed to transform to baddeleyite at 13.7 GPa. As the pressure increased further, the TiO₂-OI phase occurred at 21.9 GPa, whereas the TiO₂-II phase disappeared at 26.3 GPa. Baddeleyite and TiO2-OI coexisted in the pressure range from 26.3 to 41.5 GPa. In decompression (Figure 4b), the TiO2-OI phase fully converted back to baddeleyite at 14.7 GPa. Upon further decompressing to 8.0 GPa, the TiO₂-II phase reoccurred. A single phase TiO₂-II was formed when the sample was decompressed to \sim 0 GPa.

The HP-Raman spectra of the originally 17.9 nm TiO₂-II are shown in Figure 5. In compression (Figure 5a), the phonon mode B_u of TiO₂-II appeared at 7.9 GPa, indicating initiation of its transition to baddeleyite.⁴¹ As the pressure increased to 14.0 GPa, the Raman peaks of the baddeleyite^{23,41} phase appeared. Upon further compression to 19.3 GPa, the Raman peaks of the TiO₂-OI phase appeared, whereas the peaks of TiO₂-II became weak and then almost disappeared at 25.4 GPa. In decompression (Figure 5b), when the pressure was decreased to 14.9 GPa, almost all of the Raman peaks came

from baddeleyite. As the pressure was further decreased to 8.3 GPa, the TiO_2 -II phase appeared, which remained as the only phase when the sample was released to \sim 0 GPa. The observed phase behaviors from the Raman spectroscopy are consistent with those by the HP-XRD (above).

3.5. High-Pressure Phase Behavior of As-Prepared **20.2** nm TiO₂-II. Representative Rietveld fittings of the HP-XRD patterns of the originally 20.2 nm TiO₂-II (sample #3) are shown in Figure S8, and the derived contents of phases identified are listed in Table S5. In compression (Figure 6a), the TiO₂-II phase started to change to baddeleyite at 16.7 GPa. As the pressure increased further, the TiO₂-OI phase appeared at 22.1 GPa, whereas the TiO₂-II phase disappeared at 29.4 GPa. In the pressure range of 29.4–40.1 GPa, baddeleyite and TiO₂-OI coexisted. In decompression (Figure 6b) from 40.1 down to 15.3 GPa, TiO₂-OI tended to convert back to baddeleyite. When the pressure was decreased to 4.8 GPa, TiO₂-II appeared. After the sample was fully released to the ambient pressure (~0 GPa), a single phase of TiO₂-II was retained.

The HP-Raman spectra of the originally 20.2 nm $\rm TiO_2\text{-}II$ are shown in Figure 7. In compression (Figure 7a), the phonon mode $\rm B_u$ of $\rm TiO_2\text{-}II^{41}$ appeared at 7.7 GPa, similar to those in samples #1 and 2 (above). After the pressure was increased to 20.2 GPa, the Raman peaks of the baddeleyite phase appeared. As the pressure was further increased to 21.8 GPa, the Raman peaks of the $\rm TiO_2\text{-}OI$ phase started to form, whereas those of $\rm TiO_2\text{-}II$ disappeared at 27.0 GPa. From 27.0 to 42.0 GPa, the Raman spectra were contributed from both the baddeleyite and $\rm TiO_2\text{-}OI$ phases. In decompression (Figure 7b) from 42.0 to 15.0 GPa, the Raman peaks of $\rm TiO_2\text{-}OI$

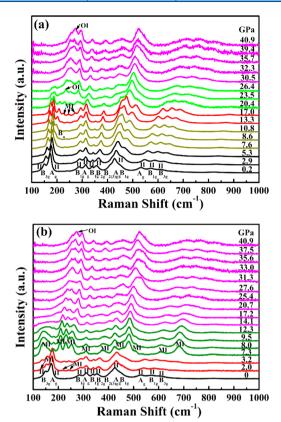


Figure 3. High-pressure Raman spectroscopy of the originally 10.7 nm TiO_2 -II (sample #1) under compression (a) and decompression (b). Neon was used as the pressure transmitting medium. II = TiO_2 -II, MI = baddeleyite, OI = TiO_2 -OI.

became weaker, while those of the baddeleyite phase became stronger. At 12.6 GPa, the Raman spectra were almost all from the baddeleyite phase. When the sample was decompressed to 6.0 GPa, the Raman peaks of TiO₂-II appeared. After the sample was fully decompressed to the ambient pressure (~0 GPa), the Raman peaks were all from the TiO₂-II phase. The observed phase behaviors from the Raman spectroscopy are consistent with those by the HP-XRD (above).

3.6. Variations of Contents, Sizes, Lattice Parameters, and Densities of Titania Phases with Pressure. From Rietveld fitting (see the examples in Figures S6-S8) of the HP-XRD data (Figures 1, 4, and 6) of the three TiO2-II samples under compression (decompression), the phase contents (Figure 8), average crystallite sizes (Figure S9), lattice parameters (Figures S10-S12), and densities (Figure S13) of relevant phases are derived as a function of pressure. The onset pressure of the phase transition from TiO2-II to baddeleyite (i.e., at the transition point) can be obtained by linear extrapolation of the phase content of baddeleyite to zero (see Figure 8). The transition pressures (~9-15 GPa) thus obtained are listed in Table 1. In the table, listed are also the average crystallite sizes and densities of TiO2-II determined from Figures S9 and S13, respectively, by reading their respective values at the corresponding transition pressures. The densities of baddeleyite at the transition pressures (Table 1) were calculated from their respective linear-least-squares fittings shown in Figure S13.

Figure 8 also shows that the TiO_2 -OI phase started to form at 18.9 (Figure 8a), 19.1 (Figure 8b), and 18.8 GPa (Figure 8c) in the three TiO_2 -II samples under compression. After

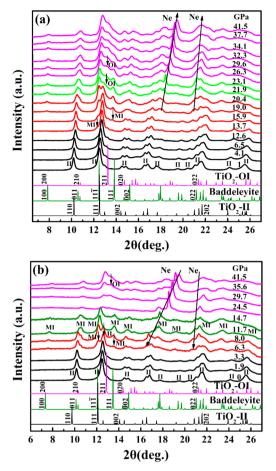


Figure 4. High-pressure XRD patterns of the originally 17.9 nm TiO_2 -II (sample #2) under compression (a) and decompression (b) using neon as the pressure transmitting medium. Calculated XRD patterns of TiO_2 -II, baddeleyite, and TiO_2 -OI are shown at the bottom for comparison. The X-ray wavelength is 0.6199 Å. II = TiO_2 -II, MI = baddeleyite, OI = TiO_2 -OI.

initiation of the formation of TiO2-OI at the transition pressure in each of the three samples, the phase content of baddeleyite continued to increase, while that of TiO2-II continued to decrease (Figure 8). This suggests that the formation of TiO₂-OI was controlled primarily by the TiO₂-IIto-TiO₂-OI transition rather than the baddeleyite-to-TiO₂-OI transition. However, after full conversion of TiO2-II to baddeleyite and/or TiO2-OI at above ~25 GPa, the phase content of baddeleyite decreased, while that of TiO2-OI increased (Figure 8), suggesting direct transition from baddeleyite to TiO2-OI. Thus, there are two parallel phase transition routes in compression of the nano TiO₂-II samples in this study: TiO_2 -II (~9-15 GPa) \rightarrow baddeleyite (~25 GPa) \rightarrow TiO₂-OI and TiO₂-II (~19 GPa) \rightarrow TiO₂-OI. In decompression, these transition sequences are reversible (Figure 8).

4. DISCUSSION

4.1. Pressure Dependence of the Average Crystallite Size of TiO_2 -II. The average crystallite sizes and microstrains of the TiO_2 -II phase in compression of the three TiO_2 -II samples are shown in Figure S9. It is seen that the average size of the TiO_2 -II phase increases with increasing pressure in sample #1 (Figure S9a), while it decreases with increasing

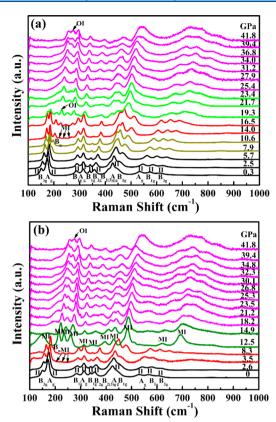


Figure 5. High-pressure Raman spectroscopy of the originally 17.9 nm TiO_2 -II (sample #2) under compression (a) and decompression (b). Neon was used as the pressure transmitting medium. II = TiO_2 -II, MI = baddeleyite, OI = TiO_2 -OI.

pressure in samples #2 and 3 (Figure S9c and e). Under compression to high pressures, there are several factors that can affect the average sizes of highly packed nanocrystallites. With an increase in pressure, nanocrystallites may undergo elastic and then plastic deformation, depending on the magnitude of the applied pressure. The former can shrink the crystallite elastically, while the latter can cause cracking of the crystallites. Both factors would produce smaller crystallite sizes with increasing pressure, as seen in Figure S9c and e. On the other hand, if adjacent nanocrystallites happen to have similar crystallographic orientations, under compression, they may join to form one or more bigger crystallites via orientated attachment. 42,43 This would produce increased crystallite sizes with increasing pressure, as seen in Figure S9a. Parts b, d, and f of Figure S9 show that, with an increase in pressure, the microstrain increases, which can be attributed to the increased structural distortions in the nanocrystallites induced by high pressure.

In order to examine the microstructures of the samples at high pressure, samples #1–3 were compressed in a DAC to their respective transition pressures (Table 1) in a neon pressure medium and then quenched to ambient pressure for TEM examinations. TEM images (Figure S14) reveal that, in the quenched samples, many original grain boundaries formed among raw anatase particles were retained, while small TiO₂-II crystallites were contained within the original grain boundaries. This once again confirms the formation of the TiO₂-II nanocrystallites from cracking and phase transition of the raw anatase particles. The average crystallite sizes (Table S6) and the size distributions (Figure S14d) derived from the TEM

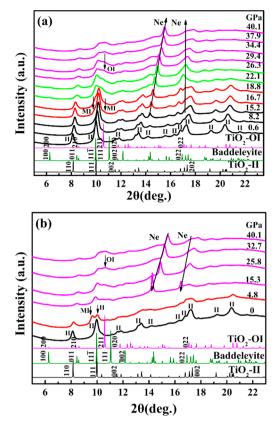


Figure 6. High-pressure XRD patterns of the originally 20.2 nm TiO_2 -II (sample #3) under compression (a) and decompression (b) using neon as the pressure transmitting medium. Calculated XRD patterns of TiO_2 -II, baddeleyite, and TiO_2 -OI are shown at the bottom for comparison. The X-ray wavelength is 0.4959 Å. II = TiO_2 -II, MI = baddeleyite, OI = TiO_2 -OI.

images are in good agreement with the sizes derived from the Rietveld fittings (Table 1).

4.2. Thermodynamic Analyses of the Size Effect on Pressure-Induced Phase Transitions. Table 1 shows that the transition pressure from TiO_2 -II to baddeleyite changes appreciably with the average crystallite size of TiO_2 -II. It has been shown previously that the size dependence of the phase transition temperature and/or pressure in nanoparticles can be analyzed using classic thermodynamics. According to ref 45, at a constant temperature, the free energy change in transition from a nanophase α (here, TiO_2 -II) to a nanophase β (here, baddeleyite) can be written as

$$\Delta G(\text{nano-}\alpha \to \text{nano-}\beta)$$

$$= \Delta G(\infty - \alpha \to \infty - \beta) + (\text{surface free energy}$$
and surface pressure contributions)
$$= \Delta G^{\circ}(\infty, T) + \Delta V(P - P_0) + 2(2t + 3)$$

$$\times M \left(\frac{\gamma_{\beta}}{D_{\beta} \rho_{\beta}} - \frac{\gamma_{\alpha}}{D_{\alpha} \rho_{\alpha}} \right)$$

$$= \Delta G^{\circ}(\infty, T) + \Delta V(P - P_0) + 10M \left(\frac{\gamma_{\beta}}{D_{\beta} \rho_{\beta}} - \frac{\gamma_{\alpha}}{D_{\alpha} \rho_{\alpha}} \right)$$

$$(1)$$

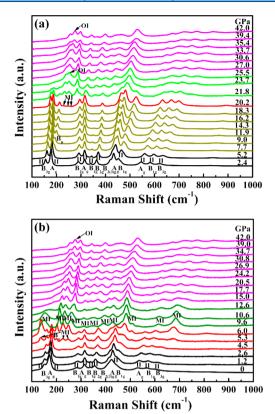


Figure 7. High-pressure Raman spectroscopy of the originally 20.2 nm TiO_2 -II (sample #3) under compression (a) and decompression (b). Neon was used as the pressure transmitting medium. II = TiO_2 -II, MI = baddeleyite, OI = TiO_2 -OI.

In the above equation, $\Delta G^{\circ}(\infty,T)$ is the free energy change from a bulk α -phase to a bulk β -phase; T is the temperature; P is the pressure (P_0 is the ambient pressure, \sim 0 GPa); M is the molecular weight of TiO_2 (79.9 g/mol); ΔV is the difference in the molar volumes of the two nanophases; t is a coefficient close to 1; and γ , D, and ρ are the interfacial energy, the diameter, and the density of a nanophase (α or β). Rigorously, γ is a function of crystallite size at a given temperature and pressure. However, it was shown that γ is insensitive to the size at larger particle sizes (e.g., $> \sim$ 10 nm for anatase)⁴⁶ and hence we treat γ as a constant in this work. ΔV can be calculated from

$$\Delta V = M \left(\frac{1}{\rho_{\beta}} - \frac{1}{\rho_{\alpha}} \right) \tag{2}$$

Thermodynamically, for occurrence of the nano ${\rm TiO_2\text{-}II\text{-}to-}$ baddeleyite transition, the free energy change (left-hand side of eq 1) must be \leq 0. Upon initiation of the phase transition (i.e., at the transition point), the free energy change equals zero. Further, as the densities of ${\rm TiO_2\text{-}II}$ and baddeleyite are close at the transition point (see Table 1), we treat $D_\alpha = D_\beta = D$. With these considerations, by substituting eq 2 into eq 1 and letting the left-hand side of eq 1 equal zero, we obtain the following relationship

$$\gamma_{\alpha}\rho_{\beta} - \gamma_{\beta}\rho_{\alpha} - \rho_{\alpha}\rho_{\beta}D \frac{\Delta G^{\circ}(\infty, T)}{10M}$$

$$= D(P_{\text{nano}} - P_{0})(\rho_{\alpha} - \rho_{\beta})/10$$
(3)

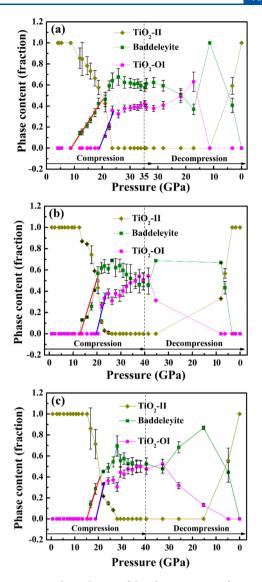


Figure 8. Pressure dependences of the phase contents of various ${\rm TiO_2}$ phases present in compression and decompression of the originally (a) 10.7 nm (sample #1), (b) 17.9 nm (sample #2), and (c) 20.2 nm (sample #3) ${\rm TiO_2}$ -II. Neon was used as the pressure transmitting medium.

Table 1. Properties of Phases at the ${\rm TiO_2}$ -II-to-Baddeleyite Phase Transition Point

sample no.	average size of TiO ₂ -II (nm)	density of TiO_2 -II (g/cm^3)	density of baddeleyite (g/cm³)	transition pressure (GPa)
1	11.0 ± 0.2^a	4.480	4.780	8.7
2	12.4 ± 0.4	4.573	4.901	13.2
3	13.1 ± 0.5	4.607	4.935	15.4
^a Standard deviation.				

or

$$P_{\text{nano}} - P_0 = \frac{10(\gamma_{\alpha}\rho_{\beta} - \gamma_{\beta}\rho_{\alpha})}{D(\rho_{\alpha} - \rho_{\beta})} + \frac{\rho_{\alpha}\rho_{\beta}}{\rho_{\beta} - \rho_{\alpha}} \frac{\Delta G^{\circ}(\infty, T)}{M}$$
(4)

where $P_{\rm nano}$ represents the transition pressure in a nanophase. For a transition at the bulk sizes, $D \to \infty$ and eq 4 becomes

$$P_{\infty} - P_0 = \frac{\rho_{\alpha} \rho_{\beta}}{\rho_{\beta} - \rho_{\alpha}} \frac{\Delta G^{\circ}(\infty, T)}{M}$$
(5)

where P_{∞} represents the transition pressure in a bulk phase. Subtracting eq 5 from eq 4, one obtains

$$P_{\text{nano}} - P_{\infty} = -\frac{10}{D} \frac{\left(\frac{\gamma_{\beta}}{\rho_{\beta}} - \frac{\gamma_{\alpha}}{\rho_{\alpha}}\right)}{\left(\frac{1}{\rho_{\beta}} - \frac{1}{\rho_{\alpha}}\right)}$$
(6)

Using known quantities at the transition points for the three ${\rm TiO_2}$ -II samples (Table 1), three concurrent equations can be established in the form of eq 3. Thus, the three unknown quantities γ_{α} , γ_{β} , and $\Delta G^{\circ}(\infty,T)$ can be derived: $\gamma_{\alpha}=3.61~{\rm J/m^2}$, $\gamma_{\beta}=0.96~{\rm J/m^2}$, and $\Delta G^{\circ}(\infty,298~{\rm K})=53675.6~{\rm J/mol}$. Understandably, the three derived quantities may have large uncertainties, as the number (three) of the established concurrent equations is just equal to the number (three) of unknown variables. Even so, the following term

$$\frac{\gamma_{\beta}}{\rho_{\beta}} - \frac{\gamma_{\alpha}}{\rho_{\alpha}} \approx -0.6 < 0$$

predicts a decrease of the transition pressure with decreasing crystallite size according to eq 6, consistent with the experimental data (Table 1).

Using the experimentally determined densities (Table 1) and the derived $\Delta G^{\circ}(\infty, 298 \text{ K})$, the transition pressure from bulk $\mathrm{TiO_2}\text{-II}$ to bulk baddeleyite was calculated to be ~47 GPa using eq 5. In a previous work, the enthalpies of various $\mathrm{TiO_2}$ phases were calculated as a function of pressure using density-functional theory. Using the enthalpy versus pressure diagram in ref 20, the theoretical transition pressure from bulk $\mathrm{TiO_2}\text{-II}$ to baddeleyite is ~25 GPa. Thus, the modeling-derived P_{∞} (~47 GPa) has the same order of magnitude as the theoretically derived one. The apparent difference between them can be attributed to the potentially high error of $\Delta G^{\circ}(\infty, 298 \text{ K})$ introduced in its derivation from only three concurrent equations (eq 3).

For the TiO_2 -II-to- TiO_2 -OI transition, the closeness in the transition pressures (18.9, 19.1, and 18.8 GPa) in the three TiO_2 -II samples suggests that

$$\frac{\gamma_{\beta}}{\rho_{\beta}} - \frac{\gamma_{\alpha}}{\rho_{\alpha}} \sim 0$$

according to eq 1, where α and β denote TiO₂-II and TiO₂-OI, respectively. Taking $\rho_{\alpha} \sim 4.6$ g/cm³ (Table 1) and $\rho_{\beta} \sim 5.3$ g/cm³,8 $\gamma_{\beta} \sim 3.61 \times 5.3/4.6 = 4.2$ J/m² according to the above relationship.

The above thermodynamic analyses show that the dissimilar pressure dependences of the phase transitions that occurred in compression of ${\rm TiO_2}$ -II nanocrystallites stem from the different interfacial energies of the involved phases, which control their thermodynamic stabilities at different sizes.

5. CONCLUSIONS

In this work, we prepared densely packed nanocrystallites of TiO_2 -II with average sizes of $\sim 10-20$ nm via high-pressure and high-temperature processing of $\sim 35-120$ nm anatase particles. Then, using in situ synchrotron XRD and Raman spectroscopy, we studied the phase transitions of the prepared TiO_2 -II nanocrystallites at pressures up to $\sim 35-40$ GPa at

room temperature. It was found that smaller raw anatase particles produced larger TiO2-II nanocrystallites. Under compression, the pressure-induced phase transitions of the TiO₂-II nanocrystallites follow the routes of nano TiO₂-II $(\sim 9-15 \text{ GPa}) \rightarrow \text{baddeleyite } (\sim 25 \text{ GPa}) \rightarrow \text{TiO}_2\text{-OI} \text{ and}$ nano TiO₂-II (\sim 19 GPa) \rightarrow TiO₂-OI, which are reversible in decompression to the ambient pressure. Thermodynamic analyses show that the decrease in the transition pressure of the TiO2-II-to-baddeleyite transition with the decrease in the crystallite size originates from the higher interfacial energy of the TiO₂-II phase (3.61 J/m²) than the baddeleyite phase (0.96 J/m²). On the other hand, the minor size dependence of the transition pressure of the TiO2-II-to-TiO2-OI transition indicates that the two phases have closer interfacial energies $(3.6 \text{ vs } 4.2 \text{ J/m}^2)$. This work enriches our understanding of the complex phase behaviors of the TiO2 system, providing knowledge useful for exploring new applications of the pressure-quenchable TiO2-II nanophase.

ASSOCIATED CONTENT

S Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcc.9b09932.

Average crystallite sizes of the raw anatase samples and the as-prepared TiO₂-II samples, SEM images and EDS elemental mapping of TiO₂-II samples, representative Rietveld fitting of HP-XRD patterns of TiO₂-II samples, pressure dependence of the crystal size of the TiO₂-II phase, lattice parameters of various TiO₂ phases present in compression and decompression of TiO₂-II samples, densities of TiO₂-II and baddeleyite phases as a function of pressure, and TEM images of TiO₂-II crystallites quenched from the transition point (PDF)

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Notes

The authors declare no competing financial interest.

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REFERENCES

- (1) Jin, X.; Yuan, K.; Wang, X.; Zhang, G.; Zhu, L.; Xu, D. High-Efficient Photocatalytic Performance under Visible Light of Functionalized TiO2 Nanofibers via Steam and Pressure Co-Modification. J. Phys. Chem. C 2019, 123, 17306-17317.
- (2) Wang, Z.; Wang, Y.; Zhang, W.; Wang, Z.; Ma, Y.; Zhou, X. Fabrication of TiO₂(B)/Anatase Heterophase Junctions at High Temperature via Stabilizing the Surface of TiO₂(B) for Enhanced Photocatalytic Activity. J. Phys. Chem. C 2019, 123, 1779-1789.
- (3) Liu, G.; Sun, C.; Cheng, L.; Jin, Y.; Lu, H.; Wang, L.; Smith, S. C.; Lu, G. Q.; Cheng, H. M. Efficient Promotion of Anatase TiO2 Photocatalysis via Bifunctional Surface-Terminating Ti-O-B-N Structures. J. Phys. Chem. C 2009, 113, 12317-12324.
- (4) Ghosh, S. K. In Functional Coatings; Ghosh, S. K., Ed.; Wiley-VCH Verlag GmbH & Co. KGaA: Weinheim, Germany, 2006; pp 1-28.
- (5) Liu, J.; Yan, J.; Shi, Q.; Dong, H.; Zhang, J.; Wang, Z.; Huang, W.; Chen, B.; Zhang, H. Pressure Dependence of Electrical Conductivity of Black Titania Hydrogenated at Different Temperatures. J. Phys. Chem. C 2019, 123, 4094-4102.
- (6) Miao, J.; Miyauchi, M.; Simmons, T. J.; Dordick, J. S.; Linhardt, R. J. Electrospinning of Nanomaterials and Applications in Electronic Components and Devices. J. Nanosci. Nanotechnol. 2010, 10, 5507-
- (7) Fan, J. C.; Bachner, F. J.; Foley, G. H.; Zavracky, P. M. Transparent Heat-Mirror Films of TiO2/Ag/TiO2 for Solar Energy Collection and Radiation Insulation. Appl. Phys. Lett. 1974, 25, 693-
- (8) Zhang, H.; Banfield, J. F. Structural Characteristics and Mechanical and Thermodynamic Properties of Nanocrystalline TiO2. Chem. Rev. 2014, 114, 9613-9644.
- (9) Marchand, R.; Brohan, L.; Tournoux, M. TiO₂(B) a New Form of Titanium Dioxide and the Potassium Octatitanate K₂Ti₈O₁₇. Mater. Res. Bull. 1980, 15, 1129-1133.
- (10) Latroche, M.; Brohan, L.; Marchand, R.; Tournoux, M. New Hollandite Oxides: TiO₂(H) and K_{0.06}TiO₂. J. Solid State Chem. **1989**, *81*, 78–82.
- (11) Akimoto, J.; Gotoh, Y.; Oosawa, Y.; Nonose, N.; Kumagai, T.; Aoki, K.; Takei, H. Topotactic Oxidation of Ramsdellite-Type Li_{0.5}TiO₂, a New Polymorph of Titanium Dioxide: TiO₂(R). J. Solid State Chem. 1994, 113, 27-36.
- (12) Hellenbrandt, M. The Inorganic Crystal Structure Database (ICSD)—Present and Future. Crystallogr. Rev. 2004, 10, 17-22.
- (13) Gražulis, S.; Chateigner, D.; Downs, R. T.; Yokochi, A. F. T.; Quirós, M.; Lutterotti, L.; Manakova, E.; Butkus, J.; Moeck, P.; Le Bail, A. Crystallography Open Database-an Open-Access Collection of Crystal Structures. J. Appl. Crystallogr. 2009, 42, 726-729.
- (14) Mattesini, M.; De Almeida, J.; Dubrovinsky, L.; Dubrovinskaia, N.; Johansson, B.; Ahuja, R. High-Pressure and High-Temperature Synthesis of the Cubic TiO₂ Polymorph. Phys. Rev. B: Condens. Matter Mater. Phys. 2004, 70, 212101.
- (15) Dekura, H.; Tsuchiya, T.; Kuwayama, Y.; Tsuchiya, J. Theoretical and Experimental Evidence for a New Post-Cotunnite Phase of Titanium Dioxide with Significant Optical Absorption. Phys. Rev. Lett. 2011, 107, No. 045701.
- (16) Razavi-Khosroshahi, H.; Edalati, K.; Hirayama, M.; Emami, H.; Arita, M.; Yamauchi, M.; Hagiwara, H.; Ida, S.; Ishihara, T.; Akiba, E.; et al. Visible-Light-Driven Photocatalytic Hydrogen Generation on Nanosized TiO2-II Stabilized by High-Pressure Torsion. ACS Catal. **2016**, *6*, 5103–5107.
- (17) Edalati, K.; Wang, Q.; Eguchi, H.; Razavi-Khosrohahi, H.; Emami, H.; Yamauchi, M. Impact of TiO2-II Phase Stabilized in

- Anatase Matrix by High-Pressure Torsion on Electrocatalytic Hydrogen Production. Mater. Res. Lett. 2019, 7, 334-339.
- (18) Möls, K.; Aarik, L.; Mändar, H.; Kasikov, A.; Niilisk, A.; Rammula, R.; Aarik, J. Influence of Phase Composition on Optical Properties of TiO2: Dependence of Refractive Index and Band Gap on Formation of TiO2-II Phase in Thin Films. Opt. Mater. 2019, 96, 109335.
- (19) Dubrovinskaia, N. A.; Dubrovinsky, L. S.; Ahuja, R.; Prokopenko, V. B.; Dmitriev, V.; Weber, H. P.; Osorio-Guillen, J.; Johansson, B. Experimental and Theoretical Identification of a New High-Pressure TiO₂ Polymorph. Phys. Rev. Lett. 2001, 87, 275501.
- (20) Liu, W.; Chen, J.; Zhang, X.; Yan, J.; Hou, M.; Kunz, M.; Zhang, D.; Zhang, H. Pressure-Induced Phase Transitions of Natural Brookite. ACS Earth Space Chem. 2019, 3, 844-853.
- (21) Al-Khatatbeh, Y.; Lee, K. K.; Kiefer, B. Compressibility of Nanocrystalline TiO₂ Anatase. J. Phys. Chem. C 2012, 116, 21635-
- (22) Dubrovinsky, L. S.; Dubrovinskaia, N. A.; Swamy, V.; Muscat, J.; Harrison, N. M.; Ahuja, R.; Holm, B.; Johansson, B. Materials Science: The Hardest Known Oxide. Nature 2001, 410, 653.
- (23) Hearne, G. R.; Zhao, J.; Dawe, A. M.; Pischedda, V.; Maaza, M.; Nieuwoudt, M. K.; Kibasomba, P.; Nemraoui, O.; Comins, J. D.; Witcomb, M. J. Effect of Grain Size on Structural Transitions in Anatase TiO2: A Raman Spectroscopy Study at High Pressure. Phys. Rev. B: Condens. Matter Mater. Phys. 2004, 70, 134102.
- (24) Swamy, V.; Kuznetsov, A.; Dubrovinsky, L. S.; McMillan, P. F.; Prakapenka, V. B.; Shen, G.; Muddle, B. C. Size-Dependent Pressure-Induced Amorphization in Nanoscale TiO2. Phys. Rev. Lett. 2006, 96, 135702.
- (25) Li, Q.; Cheng, B.; Yang, X.; Liu, R.; Liu, B.; Liu, J.; Chen, Z.; Zou, B.; Cui, T.; Liu, B. Morphology-Tuned Phase Transitions of Anatase TiO2 Nanowires under High Pressure. J. Phys. Chem. C 2013, 117, 8516-8521.
- (26) Swamy, V.; Kuznetsov, A. Y.; Dubrovinsky, L. S.; Kurnosov, A.; Prakapenka, V. B. Unusual Compression Behavior of Anatase TiO₂ Nanocrystals. Phys. Rev. Lett. 2009, 103, No. 075505.
- (27) Swamy, V.; Kuznetsov, A.; Dubrovinsky, L. S.; Caruso, R. A.; Shchukin, D. G.; Muddle, B. C. Finite-Size and Pressure Effects on the Raman Spectrum of Nanocrystalline Anatase TiO2. Phys. Rev. B: Condens. Matter Mater. Phys. 2005, 71, 184302.
- (28) Chang, H. C.; Chang, S. C.; Hung, T. C.; Jiang, J. C.; Kuo, J. L.; Lin, S. H. A. High-Pressure Study of the Effects of TiO₂ Nanoparticles on the Structural Organization of Ionic Liquids. J. Phys. Chem. C 2011, 115, 23778-23783.
- (29) Machon, D.; Le Bail, N.; Hermet, P.; Cornier, T.; Daniele, S.; Vignoli, S. Pressure-Induced Phase Transitions in TiO₂ Rutile Nanorods. J. Phys. Chem. C 2019, 123, 1948-1953.
- (30) Arlt, T.; Bermejo, M.; Blanco, M. A.; Gerward, L.; Jiang, J. Z.; Olsen, J. S.; Recio, J. M. High-Pressure Polymorphs of Anatase TiO₂. Phys. Rev. B: Condens. Matter Mater. Phys. 2000, 61, 14414.
- (31) Shul'ga, Y. M.; Matyushenko, D. V.; Golyshev, A. A.; Shakhrai, D. V.; Molodets, A. M.; Kabachkov, E. N.; Kurkin, E. N.; Domashnev, I. A. Phase Transformations in Nanostructural Anatase TiO2 under Shock Compression Conditions Studied by Raman Spectroscopy. Tech. Phys. Lett. 2010, 36, 841-843.
- (32) Lv, S. J.; Cui, H. L.; Du, K. The Pressure Performance of a Slide-Style Multianvil Large Volume Press. Adv. Mater. Res. 2013, 834-836, 1373-1376.
- (33) Lutterotti, L.; Bortolotti, M. Object Oriented Programming and Fast Computation Techniques in Maud, a Program for Powder Diffraction Analysis Written in Java. IUCr: Compcomm Newsletter 2003, 1, 43-50.
- (34) Lutterotti, L.; Matthies, S.; Wenk, H. R. MAUD: A Friendly Java Program for Material Analysis Using Diffraction. IUCr: Newsletter of the CPD 1999, 21, 14-15.
- (35) Mao, H. K.; Bell, P. M.; Shaner, J. T.; Steinberg, D. J. Specific Volume Measurements of Cu, Mo, Pd, and Ag and Calibration of the Ruby R1 Fluorescence Pressure Gauge from 0.06 to 1 Mbar. J. Appl. Phys. 1978, 49, 3276-3283.

- (36) Prescher, C.; Prakapenka, V. B. DIOPTAS: A Program for Reduction of Two-Dimensional X-Ray Diffraction Data and Data Exploration. *High Pressure Res.* **2015**, *35*, 223–230.
- (37) Jiang, H. G.; Rühle, M.; Lavernia, E. J. On the Applicability of the X-Ray Diffraction Line Profile Analysis in Extracting Grain Size and Microstrain in Nanocrystalline Materials. *J. Mater. Res.* **1999**, *14*, 549–559.
- (38) Chen, B.; Zhang, H.; Dunphy-Guzman, K. A.; Spagnoli, D.; Kruger, M. B.; Muthu, D. V. S.; Kunz, M.; Fakra, S.; Hu, J. Z.; Guo, Q. Z.; et al. Size-Dependent Elasticity of Nanocrystalline Titania. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2009**, 79, 125406.
- (39) Desgreniers, S.; Lagarec, K. High-Density ZrO₂ and HfO₂: Crystalline Structures and Equations of State. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1999**, 59, 8467.
- (40) Leger, J. M.; Atouf, A.; Tomaszewski, P.; Pereira, A. S. Pressure-Induced Phase Transitions and Volume Changes in HfO₂ up to 50 GPa. *Phys. Rev. B: Condens. Matter Mater. Phys.* **1993**, 48, 93.
- (41) Cai, Y.; Zhang, C.; Feng, Y. P. Dielectric Properties and Lattice Dynamics of α -PbO₂-type TiO₂: The Role of Soft Phonon Modes in Pressure-Induced Phase Transition to Baddeleyite-type TiO₂. *Phys. Rev. B: Condens. Matter Mater. Phys.* **2011**, 84, No. 094107.
- (42) Banfield, J. F.; Welch, S. A.; Zhang, H.; Ebert, T. T.; Penn, R. L. Aggregation-Based Crystal Growth and Microstructure Development in Natural Iron Oxyhydroxide Biomineralization Products. *Science* **2000**, 289, 751–754.
- (43) Penn, R. L.; Banfield, J. F. Imperfect Oriented Attachment: Dislocation Generation in Defect-Free Nanocrystals. *Science* **1998**, 281, 969–971.
- (44) Banfield, J. F.; Zhang, H. Nanoparticles in the Environment. Rev. Mineral. Geochem. 2001, 44, 1–58.
- (45) Zhang, H.; Banfield, J. Thermodynamic Analysis of Phase Stability of Nanocrystalline Titania. *J. Mater. Chem.* **1998**, *8*, 2073–2076
- (46) Zhang, H.; Chen, B.; Banfield, J. F. The Size Dependence of the Surface Free Energy of Titania Nanocrystals. *Phys. Chem. Chem. Phys.* **2009**, *11*, 2553–2558.