



Article Investigation of the High-Pressure Behaviors of Amblygonite by Single-Crystal X-ray Diffraction, Raman Spectroscopy, and DFT Calculations

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Abstract: In the present study, we extensively explored the high-pressure behaviors and vibrational properties of amblygonite LiAlPO₄F with elevated pressures up to 34.3 GPa based on single-crystal X-ray diffraction measurements, Raman spectroscopy, and DFT calculations. The compressibility and elastic properties of amblygonite were determined first. Specifically, the obtained isothermal bulk modulus of LiAlPO₄F is 128(4) GPa and the triclinic phase exhibited anisotropic compression with axial compressibility $\beta_c > \beta_a > \beta_b$ with a ratio of 1.11:1.00:1.20. The Raman spectra showed no indication of phase transformation and were used to obtained mode Grüneisen parameters. The average Grüneisen parameter for PO₄ tetrahedral sites was smaller than for the LiO₄F sites. Our results provide new insights into the phase stability and elastic properties of lithium-fluorite granites at extreme conditions.

Keywords: amblygonite; synchrotron single-crystal X-ray diffraction; compressibility; Raman spectroscopy; lithium-fluorite granites

1. Introduction

The behaviors of lithium-fluorite minerals and their related granites under highpressure conditions have been studied broadly over a few decades, and knowledge about such minerals has important applications in tracing the pegmatite-forming process [1–4]. Amblygonite (LiAlPO₄F)–montebrasite (LiAlPO₄OH), cassiterite, and Nb-Ta oxides are the most common accessory minerals in all the dykes of the pegmatite fields, and members of the amblygonite–montebrasite series are common constitutents of Li- and F-rich granitic pegmatites [5–7]. Hence, the amblygonite–montebrasite monitor can provide some basic knowledge of the peraluminous granitic and pegmatitic melts. The distribution of fluorine between amblygonite–montebrasite solid solutions has also long been investigated during the crystallization of these magmatic phases and associated phases as well [2,8]. Therefore, the knowledge of high-pressure behaviors of amblygonite helps understand the detailed crystal chemistry of such Li-bearing granites and can reflect the fundamental distinctions in the conditions of magma origin. However, comprehensive studies on the crystal structural evolution and physical properties of amblygonite LiAlPO₄F at extreme conditions have not been fully investigated yet.

Natural faceted gemstones of amblygonite–montebrasite isomorphous series show complete solid solutions with an ideal chemical composition of LiAlPO₄(F,OH). The minerals are open-framework alumino-phosphate series with triclinic structure. As members of the amblygonite–montebrasite series are common constituents of Li and F-rich granitic



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). pegmatites, most previous studies have focused on the determination of the F contents and F/(F+OH) ratio of such solid-solution series [2,9]. Moreover, the F-OH substitution in LiAlPO₄(F,OH) has attracted much attention due to its possible variations in crystal structural and geochemical and physical properties as well [10,11]. For example, F substitution into the lawsonite framework would likely stabilize the crystal structure since it would remove the H-H repulsion [12]. Groat et al. [11] described the crystal structure of the amblygonite–montebrasite series using a *C*-centered cell and also suggested that the pseudo-monoclinic structure was topologically identical to the titanite group minerals such as lacroixite NaAlPO₄F with a monoclinic phase. Recently, the microstructure of amblygonite–montebrasite was demonstrated by Shirose and Uehare [3] using powder X-ray diffraction and transmission electron microscope techniques. However, the structural behaviors and compressibility of amblygonite at high pressures are more sparse. Further investigation is needed to study the precise and accurate structural information and vibrational properties of amblygonite LiAlPO₄F at high-pressure conditions.

In this work, we undertook high-precision, single-crystal structure determinations of amblygonite up to ~34 GPa in situ using synchrotron-based single-crystal X-ray diffraction and theoretical calculations. High-pressure vibrational properties of amblygonite were also determined by Raman spectroscopy. These results firstly provide a comprehensive understanding of the crystallographic information of such lithium-fluorite granites under high-pressure or high-temperature conditions, thus improving our knowledge of proper elastic and chemical properties of these alumino-phosphates in pegmatites and shedding new light on alkali reservoirs in the Earth's upper mantle.

2. Materials and Methods

2.1. Experimental Setup

High-quality single-crystal samples of natural, cream-colored amblygonite were used for the current study. The amblygonite sample measured in this study had the same chemical composition as that of Dias et al. [1], including 49.58% P₂O₅, 35.19% Al₂O₃, 5.89% H₂O, and 10.25% Li₂O as well as some minor components 0.02% Na₂O and 0.40% F. We screened several chips polished to ~15 μ m thickness of the sample for high-pressure measurements. At room *P-T* conditions, the LiAlPO₄F crystal was characterized with a Bruker SMART CCD diffractometer using a sealed-tube X-ray source (MoK α radiation, λ = 0.71073 Å) operating at 45 kV and 35 mA at the China University of Geosciences (Beijing).

A short symmetric-type DAC fitted with 300 μ m Boehler-Almax diamond anvils mounted into a seat with a 56° opening was used for high-pressure measurements. A 160 μ m diameter hole was drilled in a pre-indented ~45 μ m rhenium gasket with an initial thickness of 250 μ m to act as a sample chamber. The polished amblygonite crystal and a gold foil were loaded together into the sample chamber, followed by gas loading with neon as the pressure-transmitting medium using the COMPRES/GSECARS gas-loading system [13]. XRD patterns of gold were collected at each pressure before and after sample data collection [14].

In situ high-pressure single-crystal XRD experiments were conducted at up to 34.4 GPa and room temperature at the 13-BM-C experimental station of the Advanced Photon Source, Argonne National Laboratory. The incident X-ray beam at the 13-BM-C was monochromated to 0.4340 Å with a focal spot size of $15 \times 15 \ \mu\text{m}^2$. XRD patterns were recorded with a MAR165 charge-coupled device detector that was placed about 170 mm away from the sample. The experimental details were also described previously [15,16]. To obtain an adequate number of diffraction peaks of samples and increase the coverage of the reciprocal space, we collected data at four different detector positions. Wide-scan and stepped- φ exposures were collected in a rotation range from -90° to $+90^{\circ}$ with a typical exposure time of one second per degree. Data were analyzed by the APEX3 Crystallography Software Suite, VESTA software, and the SHELXL package [17–19]. *P-V* data were fitted by the EoSFit7-GUI program [20].

High-pressure Raman spectroscopy for the amblygonite was performed at up to 28.6 GPa and at room temperature using Princeton-style diamond cells with 300 μ m ultralow fluorescent diamond anvils. Rhenium gaskets were pre-indented as sample chambers to a thickness of ~40 μ m with a hole of ~160 μ m in diameter drilled by laser at the center of the indentation. The diamond cells for Raman spectroscopy were gas loaded with neon at HPSTAR and ruby was used for pressure calibration [21]. Reported pressure uncertainties reflect the difference between pressure measurements performed before and after each data collection, which did not vary by more than ±0.2 GPa. Raman spectra were collected on a Renishaw inVia reflex Raman spectrometer with a 532 nm diode-pumped solid-state laser at Peking University. The spectra were collected in black-scattering geometry using a charge-coupled device detector with a resolution of 1 cm⁻¹. All spectra were fitted with pseudo-Voigt functions to determine the peak positions.

2.2. Computer Simulations

DFT-based first-principle calculations were performed utilizing the projected augmented wave method using the Vienna Ab initio Simulation Package [22–26]. The generalized gradient approximations with the Perdew–Burke–Ernzerhof (PBE) version were adopted to treat the exchange and correlation (XC) function [27]. We employed pseudopotentials to model the ion-electron interaction. The plane wave energy cutoff was set to 800 eV and the energy convergence criterion for the electronic self-consistent calculations was 10^{-5} eV. The force difference was converged to 1×10^{-3} eV/Å (less than 0.1 GPa). The k-points grids were set as $5 \times 5 \times 4$ in the Brillouin zone for amblygonite in structural relaxation calculations using the Monkhorst–Pack method [28]. The geometry optimization was conducted from about -2 to 27 GPa at 0 K. We changed the pressure by scaling the volume of each crystalline phase. The atomic positions and unit cell parameters were allowed to relax at each given volume to obtain the minimum total energy.

3. Results

3.1. Sample Characterization

The natural sample used in this work was obtained from Divino das Laranjeiras, the district of Linópolis, Minas Gerais in Brazil; the composition in this study is close to that published by Dias et al. [1] which is also from the same location. A small chip of amblygonite single crystal, extracted from a larger specimen, was used for the sample characterization with single-crystal diffraction, which agrees well with previous studies [29]. All observed reflections could be indexed to a triclinic primitive unit cell. The results confirmed that the amblygonite sample possess space group *P*-1 structure, and its lattice parameters were *a* = 5.0338(3) Å, *b* = 5.191(1) Å, *c* = 7.0160(6) Å, α = 106.63(1)°, β = 109.26(1)°, γ = 97.933(1)°, and *V* = 160.3(1) Å³. The crystallographic information file for amblygonite at room *P*-*T* is provided in the supporting information. The disorder in the Li site is caused by the substitution of F for OH; therefore, it would also give the OH/F disorder in the nearest sites within the structure [10]. The amblygonite structure is characterized by chains of corner-linked AlO₄F₂ octahedra that run parallel to the *c*-axis. These octahedral chains are linked laterally by edge-sharing PO₄ tetrahedra and larger LiO₄F-polyhedra [16] (Figure 1).

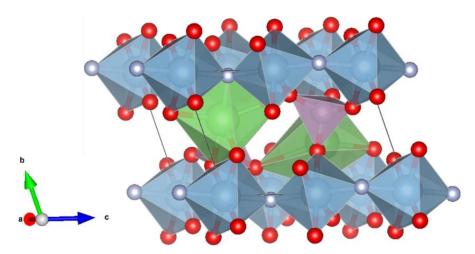


Figure 1. The crystal structure of amblygonite. Blue-colored polyhedra represent AlO₄F₂ octahedra, green-colored represent LiO₄F polyhedra, and purple-colored shapes are PO₄ tetrahedra.

3.2. Room-T compressibility

Lattice parameters and the unit–cell volume of amblygonite at high-pressure conditions were analyzed using the APEX3 v2018.7-2 software (Bruker) Figure 2 shows the single-crystal diffraction pattern at 1.0 GPa, and all diffraction spots collected can be readily indexed with the triclinic LiAlPO₄F structure. There was no indication of phase transition up to 34.4 GPa at room temperature (Table S1, see in Supplementary Materials). However, the high-pressure crystal structure could not be refined due to the limited opening angle of the diamond cell and the low symmetry of amblygonite. The obtained unit–cell reference volume, $V_{T0} = 160.27(1.7)$ Å³, is consistent with the previously reported value [29]. To obtain the EoS parameters, we then fit the *P*-*V* data to a third-order Birch–Murnaghan equation of state (BM3-EoS) using error-weighted least squares with EoSFit7c [30]. The resulting BM3-EoS parameters were as follows: $V_{T0} = 160.3(1)$ Å³, $K_{T0} = 128(4)$ GPa, and $K_{T0}' = 3.4(4)$ (Figure 2). The *P*-*V* data yielded values of $K_{T0} = 122(1)$ GPa when assuming a pressure derivative of $K_{T0}' = 4$.

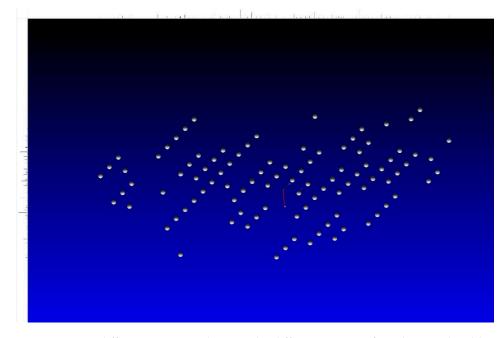


Figure 2. X-ray diffraction pattern showing the diffraction spots of single-crystal amblygonite at 1 GPa.

To verify the XRD experimental results, we then carried out the theoretical calculation using Density Functional Theory. Energy–volume results were also fitted with the BM3-EoS [31,32], which yields $V_{T0} = 163.2(1)$ Å³, $K_{T0} = 102(1)$ GPa, and $K_{T0}' = 4.2(2)$. The bulk modulus from the DFT calculation was slightly smaller than the experimental results (Figure 3). The calculated equilibrium volumes were generally underestimated by 3% in comparison to the experimental results, which is typical for PBE method computations. Our fitted values are comparable with those reported typical values of phosphates [33].

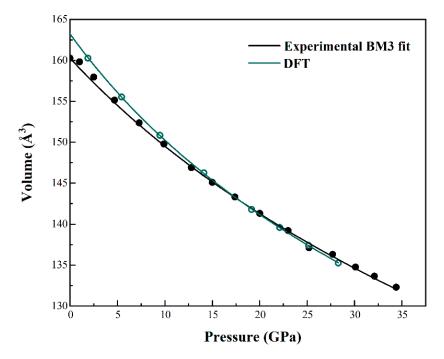


Figure 3. The volume of amblygonite as a function of pressure. Isothermal compression curves are represented by the solid lines from the BM3-EoS.

The trend of lattice parameters relative to *a* (*a*/*a*₀), *b* (*b*/*b*₀), *c* (*c*/*c*₀), *α*, *β*, and *γ* angles with pressure are plotted in Figure 3. To determine the axial compressibility of each axis in amblygonite, we used a linearized BM3 fitting where each axial dimension is cubed and treated as a volume in the BM formulation [30]. The zero-pressure axial compressibility of linear dimension *l*, defined as $\beta_{l0} = -(l^{-1})(\delta l/\delta P)_{P=0}$, is related to the linear modulus (linear incompressibility) by $K_{l0} = (\beta_{l0})^{-1}$. For amblygonite, our fitted linear moduli to *a*, *b*, and *c* were 387(7), 430(5), and 359(9) GPa, respectively, corresponding to axial compressibility values of $\beta_a = 2.58(1) \times 10^{-3}$, $\beta_b = 2.33(2) \times 10^{-3}$, and $\beta_c = 2.79(3) \times 10^{-3}$ GPa⁻¹. There is a considerable anisotropy in axial compressibility with $\beta_c > \beta_a > \beta_b$ and the ratio of zero-pressure axial compressibility in amblygonite is 1.11:1.00:1.20. The DFT calculated results are more scattering than the experimental data (experimental results: solid symbols, DFT: open circle), but both results are in agreement with each. The interaxial angles α , β , and γ showed a steady trend in compression up to ~35 GPa, supported by the experimental and calculation evidence (Figure 4).

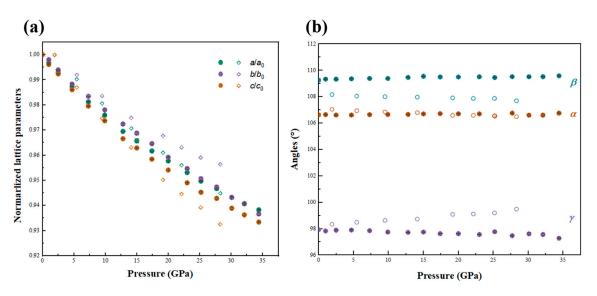


Figure 4. Pressure dependence of normalized cell lengths (*a*, *b*, and *c*) of triclinic LiAlPO₄F (**a**). Pressure dependence of internal angles (α , β , and λ) (**b**). The solid and open symbols represented the results from single-crystal X-ray measurements and DFT calculations, respectively.

3.3. Polyhedral Compression and Distortion

Bond lengths, angles, and polyhedral volumes are useful parameters to characterize the distortion of each polyhedron. The compressibilities calculated based on theoretical (DFT) results of three polyhedra (AlO₄F₂, PO₄, and LiO₄F) are significant. There were two distinct octahedral sites (Al1 and Al2), two distorted hexahedral sites (Li1 and Li2), and two P positions (P1 and P2) (Table S2). Bond length (Å), polyhedral volume (Å³), distortion index (*D*), and quadratic (λ) and bond angle variance (σ^2) for various polyhedra at different pressures are shown in Table S2.

Among these three types of polyhedra, PO₄ tetrahedra showed little or no compression, while LiO₄F polyhedra showed the greatest compression (Figure 5). The average AlO₄F₂ volume was 9.125 Å³ at 1.9 GPa and decreased to 7.725 Å³ at 28.3 GPa, and the average volume in LiO₄F polyhedra was about 7.072 Å³ at 1.9 GPa and changed to 5.377 Å³ at the highest pressure. Between 1.9 and 28.3 GPa, the PO₄ tetrahedra showed the least compression, decreasing from 1.919 to 1.793 Å³ in the amblygonite sample. Slopes of the polyhedral volumes as a function of pressure were obtained from a linear fit. It can be concluded that the distorted trigonal prismatic geometry of the LiO₄F unit is more compressible than the PO₄ rigid polyhedral unit. On the other hand, the partial replacement of Li by Na might decrease Li-O bond strength, thus making the LiO₄F polyhedra. Therefore, the unit–cell volume decrease on compression is dominated by the compression of the AlO₄F₂ octahedra and LiO₄F polyhedra.

We first calculated the distortion index, quadratic elongation, and bond angle variance to quantify the distortion of each polyhedron. The distortion index (*D*), defined as $D = \frac{1}{n} \sum_{i=1}^{n} \frac{l_i - l_{av}}{l_{av}}$, where l_i is the distance from the central cation to the ith surrounding oxygen and l_{av} is the average distance. Quadratic elongation (λ) and bond angle variance (σ^2) were employed to describe the deviation from the regular shape of polyhedra [34,35]. The bond angle variance and quadratic elongation were defined as $\sigma^2 = \sum_{i=1}^{n} \frac{(\theta_i - \theta_0)^2}{n-1}$ and $\lambda = \sum_{i=1}^{n} \frac{(l_i - l_0)^2}{n}$, respectively, where θ_i is the ith angle, θ_0 is the ideal bond angle for the perfect regular polyhedron, l_i is the ith center-to-vertex distance, and l_0 is the ith center-to-vertex distance for the regular polyhedron.

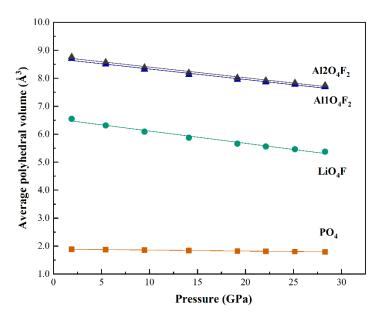


Figure 5. Pressure dependence of the average octahedral and tetrahedral volumes in amblygonite.

As a consequence, the degree of distortion within the LiO₄F polyhedra showed a significant increase with pressure, while the other AlO₄F₂ octahedra and PO₄ tetrahedra showed little or no increase as indicated by the *D* values (Figure 6). At 1.9 GPa, both the AlO₄F₂ and PO₄ polyhedra in LiAlPO₄F were close to being regular with average *D* = 0.006 and changes to 0.014 and 0.005 at 28.3 GPa, respectively. The evolutions of the values of σ^2 and λ for AlO₄F₂ and PO₄ polyhedra showed similar trends as the pressure changed (Figure 7). The σ^2 value of PO₄ tetrahedra slowly reduced from 12.25 at 1.9 GPa to 11.25 at 28.3 GPa (for λ value, from 1.0032 to 1.0029), and then increased to 13.96 (1.0035 for the λ value) at the highest pressure. The resulting values of σ^2 and λ for AlO₄F₂ octahedra were more responsive to pressure change than the PO₄ tetrahedra. The λ value of Al₂O₄F₂ octahedra rapidly increased from 1.001 to 1.0096 (for σ^2 , from 3.50 to 34.19) between 1.9 and 28.3 GPa, while the values of σ^2 and λ for Al1O₄F₂ octahedra displayed a moderate trend as pressure elevated, which increased from 1.0022 to 1.0034 and from 6.57 to 9.09 for λ and σ^2 , respectively. (Figure 6). This difference is likely due to the different structural configurations in the two distinct Al sites.

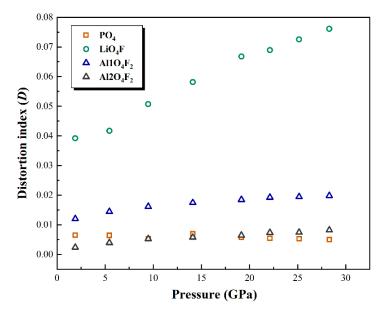


Figure 6. The pressure dependence of the distortion index (D) in amblygonite.

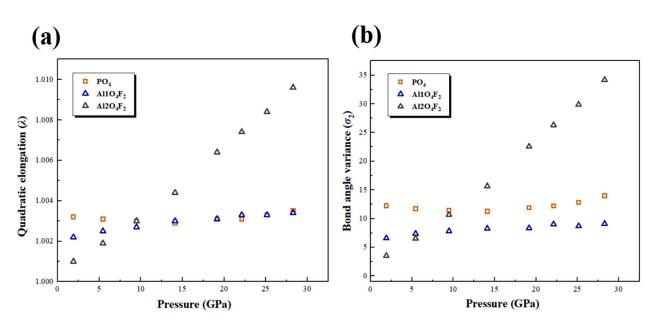


Figure 7. The pressure dependence of the quadratic elongation (λ) (**a**) and bond angle variance (σ^2) (**b**) in amblygonite, respectively.

3.4. Vibrational Properties

To date, there is no detailed high-pressure Raman spectroscopic study on amblygonite. Figure 8 shows in situ Raman spectra of LiAlPO₄F recorded from ~100 to 1300 cm⁻¹ at various pressures up to 28.6 GPa. All observed Raman peaks shifted to a higher frequency with increasing pressure. In the 1000–1150 $\rm cm^{-1}$ region, there were prominent peaks located at 1019, 1053, 1066, and 1116 cm⁻¹ that can be assigned to various P–O stretching modes [36]. The spectra were more complex below 650 cm⁻¹, and the mixed region composed of P–O bending and AlO₄F₂ stretching vibrations mainly contributed to the absorption in this domain [37]; therefore, some vibration modes merged together with increasing pressure. The intense band at 486 cm⁻¹ is attributed to the symmetric Al–O–Al stretching mode in the network. Some Raman modes located between 400–650 cm^{-1} may be assigned to the O-P-O deformation modes, which are in accordance with the results from Cooper et al. [38]. Lower frequencies from 140 to 330 cm⁻¹ can be attributed to the O–Li–O (or F) bending and Li–O bond vibrations. which are in agreement with the spectroscopic study of lithium pyroxenes [39,40]. This shows that modes v1, v2, and v3 spread out non-monotonically with increasing pressure and it might be caused by the asymmetric stretching and bending of O-Li-O and O-Li-F bonds (Figure 8). It should be noted that there were no obvious peaks broadening observed for all spectra, indicating that the structural disorder over the lattice sites was insignificant up to the highest pressure.

Grüneisen parameters (γ_i) describe the effect of changing volume of solid matter on vibrational motions of atoms; thus, the γ_i , particularly its volume dependence, is profound in the field of thermoelastic properties of solids. Mode Grüneisen parameters (γ_i) were calculated using $\gamma_i = (K_0/\nu_i) (d_{\nu_i}/d_P)_T$, where ν_i is the wavenumber of the *i*th mode and K_0 is the bulk modulus at room temperature. Here, we used the isothermal bulk modulus K_0 of 128(4) GPa for amblygonite to calculate the mode Grüneisen parameters. The resulting mean pressure coefficient of the whole structure for LiAlPO₄F was 2.22(3) cm⁻¹/GPa, and correspondingly, the calculated mode Grüneisen parameters determined in this study ranged from 0.22(1) to 1.44(2), with average value from all observed bands of 0.62(2). As for the PO₄ tetrahedral site vibrations, the calculated γ values generally fell in the range of 0.43(2)–0.44(2), and were smaller than the 0.97(3) found in LiO₄F polyhedral sites.

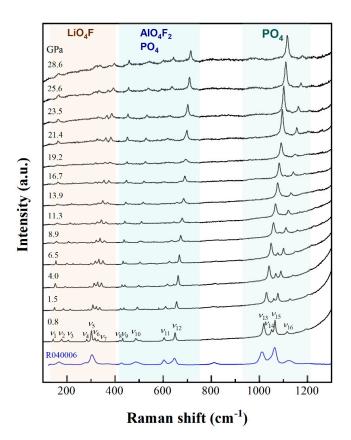


Figure 8. The Raman spectra of amblygonite at various pressures. Raman pattern from the RRUFF database (#R040006) for amblygonite is also shown for comparison.

The amblygonite–montebrasite series from petalite-bearing localities can include various contents of lacroixite, while the lower-temperature pegmatite with spodumene LiAlSi₂O₆ either did not possess or involved very low lacroixite contents [3]. Some researchers also indicated that the fluorine contents had a positive correlation with the sodium contents in the amblygonite–montebrasite series [11]. Moreover, the enriched fluxing components such as Li, F, and P in the amblygonite–montebrasite series can provide relevant information on the crystallization of the fluxing component during pegmatite formation. Although alkalis, such as lithium and sodium, are significantly enriched in continental crust compared with oceanic crust, Li and Na are important incompatible elements in the upper mantle [41,42]. Silicates are almost the exclusive hosts for Li, and Li⁺ and Na⁺ are expected to replace each other in the structure [43]. The detailed investigation of the structural evolution of such lithium-fluorite minerals under compression will give some insight into possible systematic trends in the amblygonite–montebrasite series and provide direct evidence on the alkali-rich minerals at extreme conditions in the pegmatite-forming process.

4. Conclusions

The high-pressure behaviors of amblygonite were investigated by synchrotron-based single-crystal XRD, Raman spectroscopy, and DFT calculations at pressures up to ~34 GPa. The isothermal pressure–volume relationship of LiAlPO₄F is described by the BM3-EoS, yielding $K_{T0} = 128(4)$ GPa, and $K_{T0}' = 3.4(4)$. In combination with Raman measurements performed to 28.6 GPa, we found no evidence for phase transformation over this pressure range. The OH-F substitution gave rise to the less rigid of both LiO₄F and AlO₄F₂ polyhedra and the distorted LiO₄F geometry was more compressible than the PO₄ tetrahedral unit. The average γ value of PO₄ vibration modes was 0.44(3), which is smaller than the γ value for the LiO₄F polyhedra. The findings contribute to broadening our knowledge of the crystal chemistry of amblygonite at high-pressure conditions, thus giving a better understanding of lithium-fluorite minerals and some related granites [44].

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Supplementary Materials: The following supporting information can be downloaded at: https: //www.mdpi.com/article/10.3390/cryst13081269/s1, Table S1: Lattice parameters of amblygonite at various pressures; Table S2: Bond length (Å), Polyhedral Volume (Å³), Distortion index (*D*), Quadratic (λ) and Bond angle variance (σ^2) for various polyhedra in Amblygonite at pressures up to 28.4 GPa.

Author Contributions: All authors contributed to the study conception and design. The organization of the final data and the first draft of the manuscript was written by F.Q., F.Q. and D.Z. carried out the experiments, and K.H. and F.Q. performed the data analysis and interpretation. B.H. and J.N. conducted the DFT calculations. All authors commented on previous versions of the manuscript. All authors have read and agreed to the published version of the manuscript.

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Data Availability Statement: The data used for research described in this manuscript are available upon request from corresponding author: Fei Qin (fei.qin@cugb.edu.cn).

Conflicts of Interest: The authors declare no conflict of interest.

References

- 1. Dias, L.N.; Pinheiro, M.V.B.; Moreira, R.L.; Krambrock, K.; Guedes, K.J.; Filho, L.M.; Karfunkel, J.; Scholz, R. Spectroscopic characterization of transition metal impurities in natural montebrasite/amblygonite. *Am. Mineral.* **2011**, *96*, 42–52. [CrossRef]
- London, D.; Morgan Vi, G.B.; Wolf, M.B. Amblygonite-montebrasite solid solutions as monitors of fluorine in evolved granitic and pegmatitic melts. *Am. Mineral.* 2001, 86, 225–233. [CrossRef]
- 3. Shirose, Y.; Uehara, S. Microtexture investigation of amblygonite–montebrasite series with lacroixite: Characteristics and formation process in pegmatites. *Am. Mineral. J. Earth Planet. Mater.* **2018**, *103*, 75–84. [CrossRef]
- Trunilina, V.A.; Orlov, Y.S.; Zaitsev, A.I.; Roev, S.P. High-phosphorous lithium–fluorine granites of Eastern Yakutia (Verkhoyansk– Kolyma orogenic region). *Russ. J. Pac. Geol.* 2019, *13*, 82–98. [CrossRef]
- Garate-Olave, I.; Roda-Robles, E.; Gil-Crespo, P.P.; Pesquera, A. Phosphate mineral associations from the Tres Arroyos aplitepegmatites (Badajoz, Spain): Petrography, mineral chemistry, and petrogenetic implications. *Can. Mineral.* 2020, 58, 747–765. [CrossRef]
- Roda-Robles, E.; Pesquera, A.; Gil-Crespo, P.P.; Vieira, R.; Lima, A.; Garate-Olave, I.; Martins, T.; Torres-Ruiz, J. Geology and mineralogy of Li mineralization in the Central Iberian Zone (Spain and Portugal). *Mineral. Mag.* 2016, 80, 103–126. [CrossRef]
- Roda-Robles, E.; Villaseca, C.; Pesquera, A.; Gil-Crespo, P.P.; Vieira, R.; Lima, A.; Garate-Olave, I. Petrogenetic relationships between Variscan granitoids and Li-(FP)-rich aplite-pegmatites in the Central Iberian Zone: Geological and geochemical constraints and implications for other regions from the European Variscides. Ore Geol. Rev. 2018, 95, 408–430. [CrossRef]
- 8. Veksler, I.V.; Thomas, R. An experimental study of B-, P-and F-rich synthetic granite pegmatite at 0.1 and 0.2 GPa. *Contrib. Mineral. Petrol.* **2002**, *143*, 673–683. [CrossRef]
- 9. Greiner, D.J.; Bloss, F.D. Amblygonite-montebrasite optics; response to (OH (super-)) orientation and rapid estimations of F from 2V. *Am. Mineral.* **1987**, *72*, 617–624.
- Groat, L.A.; Chakoumakos, B.C.; Brouwer, D.H.; Hoffman, C.M.; Fyfe, C.A.; Morell, H.; Schultz, A.J. The amblygonite (LiAlPO₄F)montebrasite (LiAlPO₄OH) solid solution: A combined powder and single-crystal neutron diffraction and solid-state ⁶Li MAS, CP MAS, and REDOR NMR study. *Am. Mineral.* 2003, *88*, 195–210. [CrossRef]
- 11. Groat, L.A.; Raudsepp, M.; Hawthorne, F.C.; Ercit, T.S.; Sherriff, B.L.; Hartman, J.S. The amblygonite-montebrasite series; characterization by single-crystal structure refinement, infared spectroscopy, and multinuclear MAS-NMR spectroscopy. *Am. Mineral.* **1990**, *75*, 992–1008.
- 12. Williams, Q. A vibrational spectroscopic study of hydrogen in high pressure mineral assemblages. *High-Press. Res. Appl. Earth Planet. Sci.* **1992**, *67*, 289–296.
- Rivers, M.; Prakapenka, V.B.; Kubo, A.; Pullins, C.; Holl, C.M.; Jacobsen, S.D. The COMPRES/GSECARS gas-loading system for diamond anvil cells at the Advanced Photon Source. *High Press. Res.* 2008, 28, 273–292. [CrossRef]
- 14. Dewaele, A.; Torrent, M.; Loubeyre, P.; Mezouar, M. Compression curves of transition metals in the Mbar range: Experiments and projector augmented-wave calculations. *Phys. Rev. B* **2008**, *78*, 104102. [CrossRef]
- Qin, F.; Wu, X.; Zhang, D.; Qin, S.; Jacobsen, S.D. Thermal Equation of State of Natural Ti-Bearing Clinohumite. J. Geophys. Res. Solid Earth 2017, 122, 8943–8951. [CrossRef]

- 16. Zhang, D.; Dera, P.K.; Eng, P.J.; Stubbs, J.E.; Zhang, J.S.; Prakapenka, V.B.; Rivers, M.L. High pressure single crystal diffraction at PX[^] 2 JoVE. J. Vis. Exp. 2017, 119, e54660.
- 17. Bruker. APEX3 Crystallography Software Suite, v2018.7-2; Bruker AXS Inc.: Madison, WI, USA, 2016.
- 18. Momma, K.; Izumi, F. VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Crystallogr.* **2011**, 44, 1272–1276. [CrossRef]
- 19. Sheldrick, G.M. A short history of SHELX. Acta Crystallogr. Sect. A 2008, 64, 112–122. [CrossRef]
- Gonzalez-Platas, J.; Alvaro, M.; Nestola, F.; Angel, R.J. EosFit7-GUI: A new GUI tool for equation of state calculations, analyses, and teaching. J. Appl. Crystallogr. 2016, 49, 1377–1382. [CrossRef]
- Mao, H.K.; Xu, J.; Bell, P.M. Calibration of the ruby pressure gauge to 800 kbar under quasi-hydrostatic conditions. J. Geophys. Res. 1986, 91, 4673–4676. [CrossRef]
- 22. Hohenberg, P.; Kohn, W. Inhomogeneous electron gas. Phys. Rev. 1964, 136, B864. [CrossRef]
- 23. Kohn, W.; Sham, L.J. Self-consistent equations including exchange and correlation effects. Phys. Rev. 1965, 140, A1133. [CrossRef]
- Kresse, G.; Furthmüller, J. Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set. *Comput. Mater. Sci.* 1996, 6, 15–50. [CrossRef]
- Kresse, G.; Furthmüller, J. Efficient iterative schemes for ab initio total-energy calculations using a plane-wave basis set. *Phys. Rev.* B 1996, 54, 11169. [CrossRef] [PubMed]
- 26. Kresse, G.; Hafner, J. Ab initio molecular dynamics for liquid metals. Phys. Rev. B 1993, 47, 558. [CrossRef]
- 27. Perdew, J.P.; Burke, K.; Ernzerhof, M. Generalized gradient approximation made simple. Phys. Rev. Lett. 1996, 77, 3865. [CrossRef]
- 28. Monkhorst, H.J.; Pack, J.D. Special points for Brillouin-zone integrations. Phys. Rev. B 1976, 13, 5188. [CrossRef]
- 29. Baur, W.H. Die Kristallstruktur des Edelamblygonits LiAlPO₄(OH, F). Acta Crystallogr. 1959, 12, 988–994. [CrossRef]
- Angel, R.J.; Gonzalez-Platas, J.; Alvaro, M. EosFit7c and a Fortran module (library) for equation of state calculations. *Z. Kryst.* 2014, 229, 405–419. [CrossRef]
- 31. Birch, F. Finite elastic strain of cubic crystals. Phys. Rev. 1947, 71, 809. [CrossRef]
- 32. Murnaghan, F.D. The compressibility of media under extreme pressures. Proc. Natl. Acad. Sci. USA 1944, 30, 244–247. [CrossRef]
- Errandonea, D.; Achary, S.N.; Diaz-Anichtchenko, D.; Bandiello, E.; Marqueño, T.; Shukla, R.; Tyagi, A.K.; Popescu, C.; Alabarse, F.G. Equations of State and Crystal Structures of KCaPO₄, KSrPO₄, and K₂Ce(PO₄)₂ under High Pressure: Discovery of a New Polymorph of KCaPO₄. *Cryst. Growth. Des.* 2023, 23, 2782–2794. [CrossRef]
- 34. Baur, W.H. The geometry of polyhedral distortions. Predictive relationships for the phosphate group. *Acta Crystallogr. Sect. B Struct. Crystallogr. Cryst. Chem.* **1974**, *30*, 1195–1215. [CrossRef]
- 35. Robinson, K.; Gibbs, G.V.; Ribbe, P.H. Quadratic elongation: A quantitative measure of distortion in coordination polyhedra. *Science* **1971**, *172*, 567–570. [CrossRef]
- Errandonea, D.; Gomis, O.; Rodríguez-Hernández, P.; Muñoz, A.; Ruiz-Fuertes, J.; Gupta, M.; Achary, S.N.; Hirsch, A.; Manjon, F.J.; Peters, L.; et al. High-pressure structural and vibrational properties of monazite-type BiPO4, LaPO4, CePO4, and PrPO4. J. Phys-Condens. Mat. 2018, 30, 065401. [CrossRef] [PubMed]
- Rondeau, B.; Fritsch, E.; Lefevre, P.; Guiraud, M.; Fransolet, A.M.; Lulzac, Y. A Raman investigation of the amblygonitemontebrasite series. *Can. Mineral.* 2006, 44, 1109–1117. [CrossRef]
- Cooper, M.A.; Hawthorne, F.C.; Abdu, Y.A.; Ball, N.A.; Ramik, R.A.; Tait, K.T. Wopmayite, ideally Ca₆Na₃Mn(PO₄)₃(PO₃OH)₄, a new phosphate mineral from the Tanco Mine, Bernic Lake, Manitoba: Description and crystal structure. *Can. Mineral.* 2013, *51*, 93–106. [CrossRef]
- Ding, X.; Li, J.; Chou, I.M.; Chen, Z.; Li, S. Raman spectroscopic identification of cookeite in the crystal-rich inclusions in spodumene from the Jiajika lithium pegmatite deposit, China, and its geological implications. *Eur. J. Mineral.* 2020, 32, 67–75. [CrossRef]
- 40. Pommier, C.J.S.; Denton, M.B.; Downs, R.T. Raman spectroscopic study of spodumene (LiAlSi₂O₆) through the pressure-induced phase change from C2/*c* to P21/*c*. *J. Raman Spectrosc.* **2003**, *34*, 769–775. [CrossRef]
- 41. Hofmann, A.W. Chemical differentiation of the Earth: The relationship between mantle, continental crust, and oceanic crust. *Earth Planet. Sci. Lett.* **1988**, *90*, 297–314. [CrossRef]
- 42. Tang, Y.J.; Zhang, H.F.; Deloule, E.; Su, B.X.; Ying, J.F.; Santosh, M.; Xiao, Y. Abnormal lithium isotope composition from the ancient lithospheric mantle beneath the North China Craton. *Sci. Rep.* **2014**, *4*, 4274. [CrossRef] [PubMed]
- 43. Ottolini, L.; Le Fèvre, B.; Vannucci, R. Direct assessment of mantle boron and lithium contents and distribution by SIMS analyses of peridotite minerals. *Earth Planet. Sci. Lett.* **2004**, *228*, 19–36. [CrossRef]
- 44. Gonzalez-Platas, J.; Rodriguez-Hernandez, P.; Muñoz, A.; Rodríguez-Mendoza, U.R.; Nénert, G.; Errandonea, D. A high-pressure investigation of the synthetic analogue of chalcomenite, CuSeO₃·2H₂O. *Crystals* **2019**, *9*, 643. [CrossRef]

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